

Chp 5 Little Book,
Motion Math & Work Sheet
Answers:

Be sure to show YOUR work
and the formulas for credit!

Motion Math
pages 6 & 7 in your little book

Solve the following problems. Show all
your work and attach additional paper if
necessary. Write the formulas in the
provided boxes to help. Remember to
include the correct units.

Speed & Average Speed

- *Speed Formula:*
- $S = D/T$

1. Nascar driver, Jeff Gordon, has a car that is one of the fastest on the circuit. If it travels 600 miles in 4 hours, what is his cruising speed?

$$D/T = S$$

- $600 \text{ MILES} / 4 \text{ HOURS} = 150 \text{ mph}$

2. The fastest car on Earth, a German-made Thrust SSC, would win every Nascar race in America. If it takes 0.5 hours (30 minutes) to travel 380 miles, what is its speed?

$$D/T = S$$

- $380M / 30 \text{ min} = 12.67 \text{ miles/min}$

3. The fastest train on Earth, the TGV from France, can travel at faster speeds than trains in the United States. During a speed test, the train traveled 800 miles in 2.5 hours. What is its speed?

$$D/T = S$$

- $800 \text{ m} / 2.5 \text{ hours} = 320 \text{ mph}$

4. How fast was a plane flying if it traveled 400 km in 30 min?

$$D/T = S$$

- $400 \text{ km} / 30 \text{ min} = 13.33 \text{ km/min}$

5. A Hummer travels at a speed of 50 mi/hr for 4 hrs. How far did the car travel?

$$S \times T = D$$

- $50 \text{ mph} = D / 4 = 200 \text{ miles}$
- $50 \times 4 = 200 \text{ miles}$

6. The fastest plane ever made, the Lockheed SR71, was able to travel 2200 miles per hour. Based on this speed, how far could it travel in:

a. 2 hours

$$S \times T = D$$

- $2200 = D/2 = 4400 \text{ MILES}$

b. 3 hours?

$$S/T = D$$

- $2200 = D/3 = 6600 \text{ MILES}$

c. 5 hours?

$$S \times T = D$$

- $2200 = D/5 = 11,000 \text{ MILES}$
- $2200 \times 5 = 11,000$

Velocity

- *Velocity Formula:*
- $V = D/T$

7. A car traveled 1025 km from El Paso to Dallas in 13.5 hr.
What was its average velocity?

$$V = D/T$$

- $1025 \text{ km} / 13.5 \text{ hours} = 75.93 \text{ km/hr}$
toward Dallas

8. A student walks 10 blocks to a computer store (Assume all the blocks are equal length.)

a. How long will it take him to reach the computer store if he walks 3 blocks in 2 min?

$$D/V = T$$

- $3 \text{ blocks} / 2 \text{ min} = 1.5 \text{ blocks per minute}$
 $1.5 = 10 \text{ blocks/time} = 6.67 \text{ minutes}$

b. What is his average velocity?

$$V = D/T$$

- $1.5 \text{ blocks} /$
minute toward the computer store

9. A cheetah runs at a velocity of 88 ft/sec for 40 seconds. How far does this cheetah run?

$$D = T \times V$$

- $88 \text{ ft/sec} = D/40$ $D = 3520 \text{ feet}$

Acceleration

- *Acceleration Formula:*

- $A = \frac{V_f - V_i}{T}$

10. Twenty seconds after a soccer ball is kicked (initial velocity = 0), its velocity is 32 m/s. What is its acceleration?

$$A = \frac{V_f - V_i}{T}$$

- $A = \frac{32 - 0 \text{ m/s}}{20}$
- $32/20 = 16/10 = 1.6 \text{ m/s}^2$

11. A driver starts his parked car and within 1 minute reaches a velocity of 30 mph as he travels east. What is his acceleration?

$$A = \frac{V_f - V_i}{T}$$

- $A = \frac{30-0 \text{ mph}}{1 \text{ min}} = 60 \text{ min} / 1 \text{ hr} = 1800 \text{ m/h}^2$

Random –
Find the missing
variable
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12. $V = 40 \text{ mi/hr}$ $t = 3 \text{ hrs.}$
 $D = ?$

- $V = D / T$ or $D = V \times T$
- $40 = D/3$ or $D = 40 \times 3$
- $120 \text{ MILES} = D$

13. $A = 9.8 \text{ m/s}^2$ $t = 3 \text{ hr}$
 $V = ?$

- $A = V / T$ or $V = A \times T$
- $9.8 = V/3$
- $V = 29.4 \text{ M/S}$

14. $t = 5 \text{ hr}$ $d = 100 \text{ m.}$
 $V = ?$

- $V = D/T$
- $= 100 \text{ m} / 5 \text{ hr}$
- $= 20 \text{ meters} / \text{ hr}$

15. $V = 100 \text{ mi/hr}$ $d = 400 \text{ mi}$
 $t = ?$

- $V = D/T$ or $D/V = t$
- $= 100 \text{ m / hr}$
- $= 400 \text{ miles / t}$
- $t = 4 \text{ hrs}$

A Weighty Problem

Complete this worksheet after you finish reading Chapter 5, Section 4. Pictured below are two measurement devices, A and B.

Weight or Mass?	Weight or Mass?
<ul style="list-style-type: none"> spring scale measure of gravitational force exerted on an object constant on Earth changes when gravitational force changes expressed in newtons six times less on the moon than on the Earth 	<ul style="list-style-type: none"> balance amount of matter in an object constant on Earth never changes measured in grams remains the same when gravitational force changes

A. **spring scale**

B. **balance**

- Determine whether each device measures mass or weight, and circle the correct term in each box.
- The following list contains information that relates to either mass or weight. Write each of the bulleted items in the correct boxes above. Some information may go in more than one box.
 - balance
 - spring scale
 - measure of gravitational force exerted on an object
 - amount of matter in an object
 - constant on Earth
 - measured in grams
 - changes when gravitational force changes
 - never changes
 - expressed in newtons
 - remains the same when gravitational force changes
 - six times less on the moon than on Earth

Notes: Speed-Time Graphs

Show an object's speed of accelerating over time.

Speed-Time Graph

A. Positive Acceleration
This object is getting faster & faster.

B. Negative Acceleration
This object is getting slower & slower, or decelerating.

C. No Acceleration
This object is maintaining a constant speed.

A fat line on a position-time graph means **The object has stopped moving.**

A fat line on a speed-time graph means **The object is moving at a constant speed.**

Calculating Distance
How far did this object travel in five 20 seconds?
 $D = S \times T = 150 \times 20 = 3000 \text{ m} = 3 \text{ km}$

How far did this object travel in five 9 hours?
 $D = S \times T = 30 \times 9 = 270 \text{ miles}$

Calculating Acceleration

What is the object's acceleration? 1.2 m/s^2

$\text{Acceleration} = \frac{\text{Change in Speed (m/s)}}{\text{Time (s)}}$

Comparing a Position-Time Graph to a Speed-Time Graph

Position-Time Graph

- A straight line on a position-time graph that passes through the origin indicates that the object is moving with a constant velocity.
- A curve on a position-time graph indicates that the object is accelerating.
- A horizontal line on a position-time graph indicates that the object is at rest.

Speed-Time Graph

- A horizontal line on a speed-time graph indicates that the object is moving with a constant speed.
- A line with a positive slope on a speed-time graph indicates that the object is accelerating.
- A line with a negative slope on a speed-time graph indicates that the object is decelerating.

- How far does the bus travel from the 10-second interval to the 20-second interval? **200 meters**
- What is the bus's acceleration from the second interval to the 10-second interval? **0.2 m/s²**

Speed-Time Graph #2

- How far did the bus travel from point A to point B? **100 m**
- What was the bus's speed at point C? **0 m/s**
- For how many seconds did the bus decelerate? **From 10-13 seconds, 3 seconds**
- What was the bus' acceleration from point D to point E? **1 m/s²**

Drawing a Speed-Time Graph
Marta walks at a constant speed of 6 m/s for 3 seconds. Then she runs at a constant speed of 10 m/s for 2 seconds. Create a speed-time graph using her data.

The graph below shows how the speed of a bus changes during part of a journey.

Choose the correct words from the following list to describe the motion during each segment of the journey to fill in the blanks.

- accelerating
- decelerating
- constant speed
- at rest

Segment O-A: The bus is _____ its speed changes from 0 to 10 m/s in 5 seconds.

Segment A-B: The bus is moving at a _____ of 10 m/s for 5 seconds.

Segment B-C: The bus is _____. It is slowing down from 10 m/s to rest in 3 seconds.

Segment C-D: The bus is _____. It has stopped.

Segment D-E: The bus is _____. It is gradually increasing in speed.

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- Segment O-A: accelerating
- Segment A-B: constant speed
- Segment B-C: decelerating
- Segment C-D: at rest
- Segment D-E: accelerating
- Segment E-F: constant speed

Notes: Position-Time Graphs

Show an object's position at a given time.

Position or distance on y-axis

Time on x-axis

An object moving at a constant speed creates a straight-shaped line.

The steeper an object moves, the steeper its slope.

A fat line means the object's position is not changing or the object has stopped.

A line that slopes downwards means the object is returning to its original position.

Most importantly, these graphs are used to calculate an object's speed.

$\text{Slope} = \frac{\text{Change in Position}}{\text{Change in Time}}$ $\text{Speed} = \frac{\text{Distance}}{\text{Time}}$

Interpreting a Distance-Time Graph: A runner's speed will change throughout the day, especially if a hungry lion is nearby. You can use a distance-time graph to compare the runner's speed over different time intervals.

- How far does the runner walk in the first 20 seconds? **200 meters**
- How long does the runner rest for? **20 seconds**
- What total distance does the runner travel? **280 meters**
- During what time interval did the runner travel the fastest? **From 40-60 seconds**
- What is the speed of the runner during the time interval from 0 seconds to 20 seconds? **10 m/s**
- What is the speed of the runner during the time interval from 40 seconds to 60 seconds? **8 m/s**

Interpreting a Distance-Time Graph #1

- Which runner won the race? **Albert**
- Which runner stopped for a rest? **Charlie**
- How long did he stop for? **5 seconds**
- How long did Bob take to complete the track? **14 seconds**
- Calculate Albert's average speed.
 $100 \text{ m} / 12 \text{ seconds} = 8.33 \text{ m/s}$

Drawing Position-Time Graphs

1. What is her average speed?
3 m/s

2. Is she moving at a constant speed?
Yes, even slope

3. How long did she stop for?
5 seconds

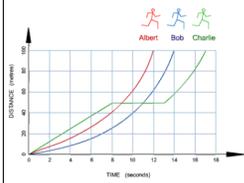
4. How long did she take to complete the track?
14 seconds

5. Calculate Albert's average speed.
 $100 \text{ m} / 12 \text{ seconds} = 8.33 \text{ m/s}$

Interpreting Position-Time Graphs Without Numbers: Describe the motion of the 3 graphs.

A: flat & steady, slows to a medium speed but steady
B: flat & steady, returns back at constant speed
C: flat, steep briefly, returns more slowly

PG16: THE RUNNERS IN DEPTH



- Which runner won the race?
-Albert won the race. He reached 100 meters first.
- Which runner stopped for a rest?
-Charlie stopped for a rest at 50m.
- How long did he stop for?
-Charlie stopped for 5 seconds. (13-8)
- How long did Bob take to finish?
-14 seconds
- Calculate Albert's average speed
 $\text{Avg speed} = \frac{\text{Total Distance}}{\text{Total time}}$
 $\frac{100\text{m}}{12\text{s}} = 8.33\text{m/s}$

Motion Graphs

Motion Graphs

Describing the motion of an object is occasionally hard to do with words. Sometimes **graphs** help make motion easier to picture, and therefore understand.

Remember:

- Motion** is a change in position measured by distance and time.
- Speed** tells us the rate at which an object moves.
- Velocity** tells the speed and direction of a moving object.
- Acceleration** tells us the rate speed or direction changes.

DISTANCE-TIME GRAPHS

Plotting distance against time can tell you a lot about motion. Let's look at the axes:

Time is shown plotted on the X-axis (bottom of the graph). The further to the right on the X-axis, the longer the time from the start.

Distance is plotted on the Y-axis (side of the graph). The higher up the graph, the further from the start.

If an object is moving at a constant speed, it means it has the same increase in distance in a given time:

Time is increasing to the right, and distance is increasing constantly with time. The object moves at a **constant speed**. **Constant speed is shown by straight lines on a graph.**

Let's look at two moving objects: Both of the lines in the graph show that each object moved the same distance, but the steeper dashed line got there before the other one:

A steeper line indicates a larger distance moved in a given time. In other words, **higher speed**. Both lines are **straight**, so both speeds are **constant**.

Graphs that show acceleration look different from those that show constant speed.

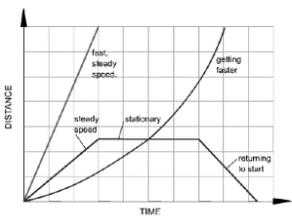
The line on this graph is curving upwards. This shows an **increase in speed**, since the line is getting steeper. In other words, in a given time, the distance the object moves is change (getting larger). It is **accelerating**.

If an object is not moving, a horizontal line is shown on a distance-time graph.

Time is increasing to the right, but its distance does not change. It is **not moving**. We say it is **At Rest**.

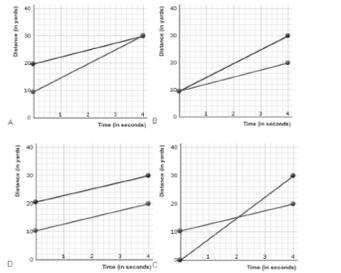
Summary:

- A distance-time graph tells us how far an object has moved with time.
- The steeper the graph, the faster the motion.
 - A horizontal line means the object is not changing its position - it is not moving, it is at rest.
 - A downward sloping line means the object is returning to the start.



(Graph from: <http://www.bbc.co.uk/schools/gcseb/te/physics/forces/speedvelocityacceleration/rev2.shtml>)

In which of the following graphs below are both runners moving at the same speed? Explain your answer.



ANSWER: Graph D

- 10. A mouse runs a distance of 2 meters in 15 seconds. What is its speed? **0.13 m/s**
- 11. Jim travelled at a speed of 18km/h for 2 hours. What was the distance covered? **36 km**
- 12. Mr. Bill was told his dinner would be ready at 6:00pm. He left the job site at (noon) 12:00pm and traveled in his car at an average speed of 45 mph to his house 300 miles away. Did Mr. Bill make it home in time for the dinner Mrs G had waiting for him?
NOPE! HE ARRIVED AT 18:40 (6:40pm) ARG!!!
A COLD dinner was waiting for him! ☹
Next time he'll need to drive a little faster! ☺

- 13. A whale swims at a constant speed of 8m/s for 17s. What distance did it travel? **136m**
- 14. Sebastian writes down his jog times for each day.
 Mon:15 min Tue:10 min Wed:12 min Thu:5 min Fri:No jog
 He jogs at a constant speed of 9km/h. Work out the distance he jogs each day. On which day did he jog the furthest?
Mon – 2.25km Tue – 1.5km Wed – 1.8km Thu – 0.75km.
He travelled furthest on Monday
- 15. How long does it take to drive a distance of 260 miles at a speed of 65mph? **4 hours**

- 16. How long does it take to travel a distance of 672km at a speed of 96km/h?
7 hours
- 17. Scripps Ranch is a distance of 135 miles away from Joshua Tree National Park. If I travelled at a constant speed of 45mph. How long would it take me to get there?
3 hours
- 18. A beetle travels at a speed of 9cm/s., it travels a distance of 108 cm before it is caught in a jar. How long did the beetle run for?
12s